# **COMMUNICATION ENGINEERING-EC8395**

# **UNIT I - ANALOG COMMUNICATION**

Communication is the process of conveying or transferring of information from one point to another point. Information can be image, text or any other data. Communication between any two points or places requires a medium in between them. This medium can be wired or wireless medium. The information that needs to be transmitted may not be in a form that is suitable for all medium. It needs to be processed. This processing of raw information to convert it into a form that is suitable for a medium is called as modulation.

# **TYPES OF COMMUNICATION**

Communication can be of two types- Analog & Digital

In Analog communication the transmit information is continuous in nature, whereas in digital communication it is discrete in nature.



Fig 1.1 Basic block diagram for communication System

Information from the source should be modulated before transmission to enable proper transmission of information from transmitter to receiver. The process of modifying or changing any characteristics of any signal is called modulation. Any signal has three characteristic they are

- 1. Amplitude
- 2. Frequency
- 3. Phase

# MODULATION:

The process of changing any one of the characteristics of carrier signal with respect to information signal is known as modulation.



Fig 1.2 Modulation

## TYPES OF MODULATION

Modulation is classified into two types they are, Analog modulation and Digital modulation. In analog modulation both information and carrier signal are analog in nature, whereas in digital information signal is digital but carrier signal is analog.



AM (Amplitude modulation):

It is the process of changing the amplitude of high frequency carrier signal in accordance with low frequency information signal. Here frequency and phase angle of carrier remains unchanged.

FM (Frequency modulation):

It is the process of changing the frequency of carrier signal accordance with amplitude of information signal.

PM (Phase modulation):

It is the process of changing the phase of carrier signal accordance with amplitude of information signal.

### NEED FOR MODULATION

- Reduce height of antenna
- Transmit signal over a long distance
- Avoid noise and interference
- Multiplexing
- Improve the signal to noise ratio

### AMPLITUDE MODULATION

It is the process of changing the amplitude of a relatively high frequency carrier signal in proportion with the instantaneous value of the modulating signal. AM is used for commercial broadcasting of audio and video signals.

Applications of AM: 1. Two-way mobile radio, Audio and video broadcast

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The modulating signal is represented as,

The carrier signal is represented as,  $e_c(t) = E_c \sin \omega_c t$ 

According to the definition, the amplitude of the carrier signal is changed after modulation.

 $e_m(t) = E_m \sin \omega_m t$ 

$$E_{AM} = E_c + e_m(t) = E_c + E_m \sin\omega_m t \qquad ------(1)$$
  
= Ec [1+ (E<sub>m</sub>/E<sub>c</sub>) sin\u03c6<sub>m</sub>t ] ------(2)  
E<sub>AM</sub> = E<sub>c</sub>(1+ m<sub>a</sub> sin \u03c6<sub>m</sub>t ) ------(3)

#### **Depth of Modulation/Modulation Index:**

Coefficient of modulation and percent modulation:

If is defined as the ratio of maximum amplitude of the message signal to the maximum amplitude of the carrier signal.

$$m_a = \frac{E_m}{E_c}$$

Percent modulation is indicated as M

$$M = \frac{E_m}{E_c} \times 100 \qquad \text{or} \qquad M = m_a \times 100$$

Relationship between m, E<sub>m</sub> & E<sub>c</sub>

From the figure.





 $\frac{1}{2} (E_{max} + E_{min})$   $E_{max} + E_{min}$ 

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Where  $m_a = E_m/E_c$  Where  $m_a$  is the modulation index (or) depth of modulation. The value  $E_m$  must be less than value of  $E_c$  to avoid distortion in the modulated signal. Hence maximum value of  $m_a$  will be equal to 1. When  $m_a$  is expressed in percentage it is called percentage modulation.

But the instantaneous amplitude of modulated signal, i.e at any time

$$e_{AM}(t) = E_{AM} \sin \omega_c t \qquad -----(4)$$

Substitute equation (3) in (4)

$$e_{AM}(t) = E_c (1 + m_a \sin \omega_m t) \sin \omega_c t$$

= Ec sin $\omega_c t$  + m<sub>a</sub> Ec sin $\omega_m t$  sin $\omega_c t$ 

(1) (2)

Expand the second term ( $sin\omega_m t sin\omega_c t$ ) according to (SinASinB) formula, we get

$$e_{AM}(t) = E_c sin\omega_c t + \frac{maE_c}{2} cos(\omega_c - \omega_m)t - \frac{maE_c}{2} cos(\omega_c + \omega_m)t \quad -----(5)$$
  
= Carrier + USB + LSB

Frequency spectrum and Bandwidth of AM Wave



- Fig 1.4 Frequen
   The figure shows the frequency spectrum of Am.
- It extends from f<sub>c</sub> -f<sub>m</sub> (max) to f<sub>c</sub> + f<sub>m</sub> (max).
- The band of frequencies b/w f<sub>c</sub> and f<sub>c</sub> f<sub>m</sub> (max) is called lower side band [LSB] and any frequency within this band is called lower side frequency [LSF].
- The band of frequencies b/w f<sub>c</sub> and f<sub>c</sub> + f<sub>m</sub> (max) is called upper side band [USB] and any frequency within this and is called upper side frequency [USF]

#### Bandwidth of AM.

The Bandwidth of Am wave is equal to the difference b/w the highest upper side frequency and lowest lower side frequency.

$$B = f_c + f_m (max) - [f_c - f_m (max)]$$

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=  $f_c + f_m (max) - f_c + f_m (max)$ 

BW = 
$$2f_m (max)$$

# **AM Waveform**



- a) Message signal
- b) Carrier signal
- c) Amplitude modulated signal.

Fig 1.5 AM Waveform The shape of modulated waveform is known as AM envelope.

# Phasor representation of AM



(i). Critical Modulation

•

- (ii). Over Modulation
- $(iii). \ \textit{Under Modulation}$
- When  $E_m = E_c$  modulation goes to 100% this situation is known as critical modulation.



• E<sub>m</sub> < E<sub>c</sub>

leads to under modulation.



• E<sub>m</sub> > E<sub>c</sub> leads to over modulation.



Envelope of AM wave for m = 3/2 Fig 1.7 AM Types based on Modulation Index AM POWER DISTRIBUTION

- The modulated wave contains three terms such as carrier wave, LSB, USB.
- The modulated wave contains more power than the unmodulated carrier. Total Power in modulated wave will be,

 $P_t = P_C + P_{USB} + P_{LSB}$ 

i.e. total power Pt of AM wave is the sum of carrier power and side band power.

 $P_C$  - Carrier power,  $P_{USB}$  - Upper Side Band power,  $P_{LSB}$  - Lower Side Band power

The carrier power is

$$P_{c} = \frac{E_{c}^{2}}{R} = \frac{(Ec / \sqrt{2})^{2}}{R} = \frac{Ec^{2}}{2R}$$

The lower and upper sideband powers are same which is given by

$$P_{USB} = P_{LSB} = \frac{(m_a E_c/ 2\sqrt{2})^2}{R} = \frac{m_a^2 E_c^2}{8R}$$

In terms of carrier power

$$P_{USB} = P_{LSB} = \frac{(m_a E_c/2\sqrt{2})^2}{R} = \frac{m_a^2 E_c^2}{8R} = \frac{m_a^2 P_c}{4}$$

 $P_t \hspace{0.2cm} = \hspace{0.2cm} P_c + \hspace{0.2cm} P_{USB} \hspace{0.2cm} + \hspace{0.2cm} P_{LSB}$ 

$$P_{t} = P_{c} + \frac{m_{a}^{2} P_{c}}{4} + \frac{m_{a}^{2} P_{c}}{4}$$

$$P_{t} = P_{c} \left(1 + \frac{m_{a}^{2}}{2}\right)$$

#### AM CURENT DISTRIBUTION

The equation of  $P_t$  given by

$$\frac{P_t}{P_c} = \begin{pmatrix} 1 & \frac{m_a^2}{2} \\ 2 \end{pmatrix}$$

$$\begin{split} P_t &= I_t^2 R \\ P_c &= I_c^2 R \\ I_t^2 &= I_c^2 \left( 1 + \frac{m_a^2}{2} \right) \\ I_t &= I_c \sqrt{1 + \frac{m_a^2}{2}} \end{split}$$

Where  $I_t = Total(or)modulated current$ ,  $I_C = Carrier current$ 

#### **Efficiency:**

% 
$$\eta = \frac{Power in side band}{Total Power} * 100$$
  

$$= \frac{P_{LSB+}P_{LSB}}{P_{Total}} * 100$$

$$= \frac{m_a^2}{2+m_a^2} * 100$$
If  $m_a = 1$ , Then %  $\eta = 33.33$  %

In this only one third of total power is carried by the sidebands and the rest two third is wasted.

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• If the modulating signal contains two frequencies say  $f_{m1} \& f_{m2}$ , the modulated wave will contain the carrier and two sets of side frequencies. Spaced symmetrically about the carrier.

$$\begin{split} V_{am}\left(t\right) = & \sin 2\pi \ fct + \frac{1}{2} \sin 2\pi \ (fc - f_{m1}) \ t - \frac{1}{2} \sin 2\pi \ (fc + f_{m1}) \ t \\ & + \frac{1}{2} \sin 2\pi \ (fc - f_{m2}) \ t - \frac{1}{2} \sin 2\pi \ (fc + f_{m2}) \ t \end{split}$$

- The coefficient of modulation or modulation index is given by  $m_t = \sqrt{m_1^2 + m_2^2}$
- In general for n different signals  $mt = \sqrt{m_1^2 + m_2^2 + \dots m_n^2}$
- $P_{usbt} = P_{lsst} = P_c m_t^2 / 4$

$$P_t = P_c (1+m_t^2/2)$$

# Advantages, Disadvantages and Applications of AM (DSBFC)

# <u>Advantages</u>

- 1. Simple and inexpensive receivers. Easy to detect with simple equipment even if the signal is not very strong
- 2. Narrow bandwidth than FM
- 3. Wider coverage
- 4. Well-established, mature art used for broadcasting almost exclusively

# **Disadvantages**

- 1. Received signal affected by electrical storms and other radio frequency interference
- 2. Receivers able to reproduce frequencies up to 5 MHz or less
- 3. Inefficient use of transmitter power

# **Applications**

1. Low quality form of modulation that is used for commercial broadcast of both audio and video signals

Carrier

- 2. Two way mobile radio communications such as citizen band (CB) radio
- 3. Aircraft communication in the VHF frequency range

# TYPES OF AM MODULATION



	LSB	USB	
5. Vestigial sideband			

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### AM modulating Circuits

- Based on the location in the transmitter AM modulating circuits are classified as
  - a. Low level AM modulator
  - b. High level AM modulator

### Difference b/w low level and High level AM mod.

Low level AM modulator	High level AM modulator
Modulation takes place prior to the final stage of the transmitter	Modulation takes place in the final element of final stage.
Less modulating signal power is required	More modulating signal power is required.

# **GENERATION OF AM-DSBFC (AM MODULATORS)**

The generation method of AM waves are broadly divided in to two types

- Linear modulator(or)large signal modulator(or)high level modulation
- Non Linear modulator(or)small signal modulator(or)low level modulation

# LINEAR MODULATOR:

In this type of modulators the devices are operated in linear region of its transfer characteristics. Linear modulators are also divided in to two types,

- Transistor modulator
- Switching modulator.

# NON LINEAR MODULATORS:

These modulators are operated in nonlinear region. These are used in low level modulation. **The types of non linear modulators are,** 

Square law modulator, Product modulator, Balanced modulator.

# LOW LEVEL AM MODULATOR

- Class A amplifier can perform amplitude modulation.
- Amplifier must have 2 inputs one for the carrier signal & second for modulating signal.
- With no modulating signal present, the circuit operates as a linear class A amplifier, and the output is simply the carrier amplified by the quiescent voltage gain .
- The carrier is applied the base and the modulating signal to the emitter. Hence it is also called as **Emitter Modulation**.
- The modulating signal varies the gain of the amplifier at a sinusoidal rate equal to the frequency of the modulating signal.
- The depth of modulation achieved is proportional to the amplitude of the modulating signal.





# (a) Circuit diagram of low level AM modulator



# Fig 1.8 Low Level AM Modulator

• The voltage gain for an emitter modulator is expressed as,

 $A_v = A_q (1 + m \sin 2\pi fmt)$ 

 $A_v \rightarrow$  Amplifier voltage gain with modulation.

 $A_q \rightarrow$  Amplifier quiescent (without modulation) voltage gain.

 $\sin 2\pi f_m t$  varies from + 1 to -1

Hence,  $A_v = A_q (1\pm m)$ 

 $Av_{max} = 2Aq,$  when m = +0 $Av_{min} = 0,$  when m = -1

• The modulating signal drives the circuit into both saturation and cutoff, thus producing the nonlinear amplification necessary for modulation to occur. The collector waveform includes the carrier and the upper

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and lower side frequencies as well as a component at the modulating signal frequency from the waveform, thus producing a symmetrical AM envelop at  $V_{out}$ .

# Advantages of Low level modulation:

- 1. Less modulating signal power is required to obtain high percentage modulation.
- 2. Modulating circuit is designed for low power.

## Disadvantage of Low level modulation

Amplifiers following modulator stage must be linear. At high operating powers linear amplifiers are very inefficient.

# HIGH POWER AM MODULATOR / MEDIUM POWER AM MODULATOR

- The class C amplifier is used. It operates nonlinear and is capable of nonlinear mixing (modulation).
- This is known as collector modulator because modulating signal is applied to the collector.
- When the amplitude of the carrier exceeds the barrier potential (0.7V) Q1 turns on collector current flows.



# Fig 1.9 High Power AM Modulator

- When carrier voltage drops below 0.7V Q1 turns off and collector current cases.
- The corresponding current and voltage waveforms are shown.
- When the modulating signal is applied it adds up with the  $Ec_c$  and gets submitted from  $Ec_c$  producing an Am o/p.

# Advantages of high level modulators:

- There is no constraint of linear operation on amplifiers preceding modulator stage.
- Power efficiency is good

# **Disadvantages of high level modulators:**

- High modulating power is required.
- Final modulating signal amplifier has to supply all the sideband power.

# AM TRANSMITTERS

# Low Level AM Transmitter

• The block diagram of a typical AM transmitter is shown in which carrier source is a crystal oscillator. The crystal oscillator is stabilized in order to maintain the carrier frequency deviation within a prescribed limit.

• The crystal oscillator is followed by a tuned buffer amplifier (class B) and drive amplifier.



Fig 1.10 Low level AM Transmitter

- The modulator circuit used is generally a class C power amplifier that is a collector modulator.
- The audio signal is amplified by a chain of low level audio amplifiers and a power amplifier. This amplifier is controlling the power being delivered to the final RF amplifier. Class B push pull amplifier is usually used for this purpose.
- The amplified modulating signal is applied to the modulator along with the carrier. AM wave is got at the output of the modulator.
- This AM signal is then amplified using a chain of linear amplifiers to raise its power level. Class B amplifiers are used for this purpose. The linear power amplifier is used to avoid the distortion in the AM wave.
- The amplitude modulated signal is then transmitted using transmitting antenna. The matching network matches the output impedance of the final amplifier to the transmission line and antenna.

<u>Application of Low Level AM Transmitter</u>: It is used in low capacity system such as wireless intercoms, Remote control units, pagers, shot range talkie.

### High Level AM Transmitter



# Fig 1.11 High level AM Transmitter •

Here modulating signal power should be higher than the low level.

• The amplification takes place prior to modulation.

# Application of High Level Transmitter: Used for long distance communications.

# SQUARE LAW MODULATOR

The non linear portion of V-I characteristics of diode is used as a element for non-linear modulators.
 This is suited at low voltage levels because of the fact that current-voltage characteristics of a diode is highly nonlinearDiode currentparticularly in the low voltage region as shown in figure





- A square law modulator has three features shown in figure.
- Summer To sum carrier and modulating signal
- > A non linear element
- > Band pass filter for extracting desired modulating products.



Fig 1.14 Components of Square Law Modulator

### Principle of operation:

Signal

- From the figure the non linear device diode is used to produce low level amplitude modulation.
- > Here the carrier and modulating signals are applied across the diode.
- A dc battery Ecc is connected across the diode to get a fixed operating point on the V-I characteristics of the diode.
- This amplitude modulation that is low level can be explained by considering the fact when two different frequencies are passed through the non linear device.
- So when we apply carrier and modulating frequencies different frequency terms appear at the output of diode.
- These different frequency terms are applied across the tuned circuit which is tuned to carrier frequency and has a narrow bandwidth just to pass two sidebands along with the carrier and reject other frequencies.

So the output of the tuned circuit will be carrier and two sidebands that is amplitude modulated wave is produced.

### Mathematical analysis:

Let the modulating voltage will be $e_m(t) = E_m \sin \omega_m t$	(1)
Let the carrier voltage will be $e_c(t) = E_c \sin \omega_c t$	(2)
So the input voltage applied to the diod $e_1(t) = e_m + ec$ $= E_m \sin \omega_m t + E_c \sin \omega_c t$	e will be (3)

We know that the current and voltage relationship of a linear circuit is,

i=av where i=current through linear device v=voltage through the linear device a=proportionality constant

- The current and voltage relationship of a nonlinear circuit may be expressed as,  $i=a V_1+b V_1^2+c V_1^3+\cdots$
- This means that due to non-linearity in the V-I characteristics of a non-linear circuits, the current becomes proportional not only to voltage but also to the square, cube and higher powers of voltage. So  $i = a_1V_1+a_2V_1^2+a_3V_1^3+$  -------(4)

Where  $a_1, a_2, a_3$  are proportionality constants and  $V_1$  is the input voltage applied to the diode or FET. Sub eqn (3) in (4)then

 $i = a_1(E_m \sin\omega_m t + E_c \sin\omega_c t) + a_2(E_m \sin\omega_m t + E_c \sin\omega_c t)^2 + \dots = a_1 Em \sin\omega_m t + a_1 Ec \sin\omega_c t + a_2 Em^2 \sin\omega_m^2 t + a_2 Ec^2 \sin\omega_c^2 t + 2a_2 EmEc \sin\omega_m t \sin\omega_c t + \dots$ 

Neglecting second and higher order terms, we get

 $i(t) = a_1 \operatorname{Em} \operatorname{sin}\omega_m t + a_1 \operatorname{Ec} \operatorname{sin}\omega_c t + a_2 \operatorname{Em}\operatorname{Ec} \operatorname{sin}\omega_m t \operatorname{sin}\omega_c t + \cdots$ 

 $= a_1 \operatorname{Em} \operatorname{sin} \omega_m t + a_1 \operatorname{Ec} \operatorname{sin} \omega_c t + a_2 \operatorname{Em} \operatorname{Ec} \left[ \cos(\omega_c - \omega_m) t - \cos(\omega_c + \omega_m) t \right]$ 

> The tuned circuit is tuned to the carrier frequency and it allows only  $\omega_c$ ,  $\omega_c + \omega_m$ ,  $\omega_c - \omega_m$  terms and eliminates all other terms.hence we obtain

 $i(t) = a_1 \text{ Ec } \sin \omega_c t + a_2 \text{EmEc } [\cos(\omega_c - \omega_m)t - \cos(\omega_c + \omega_m)t]$ 

$i(t) = a_1 \operatorname{Ec} \sin \omega_c t + a_2 \operatorname{EmEc} \cos(\omega_c - \omega_m) t - a_2 \operatorname{EmEc} \cos(\omega_c + \omega_m) t - \dots - (5)$				
(carrier)	(LSB)	(USB)		The

main drawback of using diode modulator is it does not provide amplification and a single diode is unable to balance out the frequency completely. These limitations can be eliminated by using amplifying devices like transistor, FET in a balanced mode.

> We can also use the square law modulator with FET instead of diode.

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From the final equation we know that it consists only the carrier and USB and LSB frequency components and all the components are removed.

# **BALANCE MODULATOR METHOD**

It is assumed that the two transistors are identical and the circuit is symmetrical. The operation is confined in the nonlinear region of the active devices employed in this circuit. The carrier voltage across the upper and lower part of the secondary windings of the center tap transformers are equal in magnitude and opposite in phase.



### Fig 1.15 Balanced Modulator

- > In this the carrier voltage across the two windings of a centre tap transformers are equal and opposite in phase  $V_{be} = -V_{be}$
- > Input voltage to the transistor T1 is given by,  $V_{be} = e_c(t) + e_m(t)$

$$V_{be} = E_c \sin \omega_c t + E_m \sin \omega_m t \qquad ------(1)$$

Similarly Input voltage to the transistor T2, V'<sub>be</sub> = -e<sub>c</sub>(t)+ e<sub>m</sub>(t)

$$V'_{be} = -E_c \sin \omega_c t + E_m \sin \omega_m t \qquad -----(2)$$

By using the non-linearity property the collector current can be written as per square law equation

$$i_c = a_1 V_{be} + a_2 V_{be}^2 + \dots$$
 (3)

$$i_c' = a_1 V'_{be} + a_2 V'_{be}^2 + \dots$$
 -----(4)

On substituting eqn 1 and 2 in 3 and 4 we get,

 $i_c = a_1 [E_c \sin \omega_c t + E_m \sin \omega_m t] + a_2 [E_c \sin \omega_c t + E_m \sin \omega_m t]^2$ 

 $i_c = a_1 \left[ E_c \sin \omega_c t + E_m \sin \omega_m t \right] + a_2 E_c^2 \sin^2 \omega_c t + a_2 E_m^2 \sin^2 \omega_m t + 2a_2 E_m E_c \sin \omega_m t \sin \omega_c t - --(5)$ 

 $i'_c = a_1 [-E_c \sin \omega_c t + E_m \sin \omega_m t] + a_2 [-E_c \sin \omega_c t + E_m \sin \omega_m t]^2$ 

 $i'_{c} = a_{1} \left[ -E_{c} \sin \omega_{c} t + E_{m} \sin \omega_{m} t \right] + a_{2} E_{c}^{2} \sin^{2} \omega_{c} t + a_{2} E_{m}^{2} \sin^{2} \omega_{m} t - 2a_{2} E_{m} E_{c} \sin \omega_{m} t \sin \omega_{c} t - -(6)$ 

The output AM Voltage V<sub>0</sub> is given by  $V_0 = K [i_c - i_c']$  -----(7)

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since  $i_c$ ,  $i'_c$  flows in the opposite direction and 'K' is a constant depending on impedance or other circuit parameters.

On substituting equation 5 and 6 in 7 we get,

$$\begin{split} V_o &= K \left[ i_c - i_c' \right] \\ E_o &= K \left[ 2 a_1 \operatorname{Ec} \operatorname{Sin}\omega_c t + 4 a_2 \operatorname{Em} \operatorname{Ec} \operatorname{Sin}\omega_m t \operatorname{Sin}\omega_c t \right] \\ &= 2 \operatorname{KEc} a_1 \operatorname{Sin}\omega_c t \left[ 1 + \frac{2 a_2}{a_1} \operatorname{Em} \operatorname{Sin}\omega_m t \right] \\ &= 2 \operatorname{KEc} a_1 \operatorname{Sin}\omega_c t \left[ 1 + \operatorname{ma} \operatorname{Sin}\omega_m t \right] \\ &\text{where } m_a = 2 a_2 \operatorname{Em} \text{ is the modulation index} \end{split}$$

al This equation represents the output modulated voltage which contains carrier and side band terms but no modulating terms. Thus this circuit is used as AM modulator. The advantage of this circuit is that the undesired harmonics are automatically balanced out and hence there is no need for separate filter.

# DEMODULATION/DETECTION OF AM-DSBFC (AM DEMODULATORS)

- Demodulation or detection is nothing but the process of extracting a modulating or information signal from modulated signal. Otherwise in other words, demodulation or detection is the process by which the message is recovered from the modulated signal at receiver.
- > The devices used for demodulation or detection are called as demodulators or detector
- > For amplitude modulation, the detectors or demodulators are categorized are

#### Square law detectors or nonlinear detectors Linear detectors

> The low level modulated signals are using non linear detectors to recover the original message signal

# SQUARE LAW DETECTOR

- > The square law detector circuit is used for detecting low level modulated signal.
- $\blacktriangleright$  Here the diode is used in V I characteristics of the device i.e. non linear characteristics of the diode.
- The square law detector is similar to the square law modulator. The only difference lies in the filter circuit.
- In square law modulator we are using band pass filters, in square law detector; a low pass filter is used. The operation is limited to the non-linear region of the diode characteristics, so the lower half portion of the modulated waveform is compressed.
- This produces the envelope distortion, so the average value of the diode current is no longer constant and varies with time. The average diode current consists of steady DC component and time varying modulation frequency. Due to nonlinear region the lower half of its current wave form is compressed. This may cause envelope distortion due to this diode current will not be constant, and varies with time.



# Fig 1.16 Square Law Detector

The distorted output diode current is expressed by the non-linear V-I relationship (i.e. square law) is,  $i_0=a_1 e_{AM} + a_2 e_{AM}^2$  ------(1) where  $e_{AM}=i/p$  modulated signal.

The equation of AM wave is  $\frac{1}{2}$ 

 $e_{AM} = Ec (1 + m_a \sin \omega_m t) \sin \omega_c t \quad -----(2)$ 

On substituting equation 2 in 1 we get

 $i_0 = a_1 \text{ Ec} (1 + m_a \sin \omega_m t) \sin \omega_c t ] + a_2 [\text{Ec} (1 + m_a \sin \omega_m t) \sin \omega_c t ]^2$ 

 $i_0 = a_1 \ Ec \ sin\omega_c t + a_1 \ m_a \ Ec \ sin\omega_c t \ sin\omega_m t + a_2 \ Ec^2 \ sin^2 \omega_c t \ (1 + m_a \ sin\omega_m t)^2$ 

 $=a_1 Ec sin\omega_c t + a_1 m_a Ec sin\omega_c t sin\omega_m t + a_2 Ec^2 sin^2 \omega_c t (1 + m_a^2 sin^2 \omega_m t + 2 m_a sin\omega_m t )$ 

 $= a_{1} \operatorname{Ec} \operatorname{sin} \omega_{c} t + a_{1} \operatorname{m}_{a} \operatorname{Ec} \operatorname{sin} \omega_{c} t \operatorname{sin} \omega_{m} t + a_{2} \operatorname{Ec}^{2} (1 + \operatorname{m}_{a}^{2} \operatorname{sin}^{2} \omega_{m} t + 2 \operatorname{m}_{a} \operatorname{sin} \omega_{m} t) \left( \frac{1 - \cos 2\omega_{c} t}{2} \right)$   $= a_{1} \operatorname{Ec} \operatorname{sin} \omega_{c} t + a_{1} \operatorname{m}_{a} \operatorname{Ec} \operatorname{sin} \omega_{c} t \operatorname{sin} \omega_{m} t + \frac{a_{2} \operatorname{Ec}^{2}}{2} - a_{2} \operatorname{Ec}^{2} \frac{\cos 2\omega_{c} t}{2} + \frac{a_{2} \operatorname{Ec}^{2} \operatorname{m}_{a}^{2} \sin^{2} \omega_{m} t}{2} + \frac{a_{2} \operatorname{Ec}^{2} \operatorname{m}_{a}^{2} \sin^{2} \omega_{m} t \cos 2\omega_{c} t} + a_{2} \operatorname{Ec}^{2} \operatorname{m}_{a} \operatorname{sin} \omega_{m} t - a_{2} \operatorname{Ec}^{2} \operatorname{m}_{a} \operatorname{sin} \omega_{m} t \cos 2\omega_{c} t$ 

The carrier term is filtered by using a low pass filter and high frequency term are also reduced then,  $i_0 = a_2 Ec^2 m_a sin\omega_m t$ 

So the final output contains a signal with modulating frequency. Hence original signal is recovered.

# **ENVELOPE DETECTOR**

- A detector circuit whose output follows the envelope of the modulated signal which is used to reproduce the modulating or message signal is called as "Envelope Detector".
- This is most popular commercial receiver circuits since it is very simple and not expensive, and also it gives satisfactory performance. An envelope detector of the series type is shown in Figure which consists of a diode and a resistor capacitor filter a time constant network.



Fig 1.17 Envelope Detector



# **Principle Of Operation:**

- Modulated signal is applied to the series combination of diode and the load impedance consisting of a resistor R and C.
- > Operation takes place over the linear region of VI characteristics of Diode.
- For positive cycle of carrier signal the diode D conducts thereby the capacitor charges to the peak voltage with the time constant  $\tau = \mathbf{R} \mathbf{C}$  of the carrier signal through the resistor R.
- As the input falls below the peak value, the diode reaches cut-ff. The diode acts as open switch and hence the capacitor gets discharge path through R.
- During negative half cycle the diode is reverse biased and the carrier voltage is disconnected from the RC circuit. So the capacitor discharges continuously until next positive cycle appears.
- From the peak of one positive cycle to the next the capacitor discharges slowly and this process continues. Thus the voltage across 'C' is same as the envelope of the modulated carrier but spikes are introduced. So the output voltage across capacitor is a spiky modulating or base band signal. So the envelope is detected at the output of capacitor. Thus from the average value the original signal is recovered by extracting the envelope.
- The spikes can be reduced to a negligible amount by keeping the time constant RC large so that the capacitor C discharges negligible amount.

# CHOICE OF TIME CONSTANT RC

- Large (or) small value of time constant makes problem. So time constant is important consideration.
- If time constant RC is quite low: Discharge curve during non conductive period is almost vertical, so fluctuations may occur in output voltage. This results in Diagonal clipping
- If RC is very large: Discharge curve is almost horizontal, so several peaks will be missed in the rectified output voltage. This results in negative peak clipping. Distortion in diode detector:

There are two clippings i.e. distortions available Negative peak clipping

# Diagonal clipping.

# **Diagonal clipping:**

It results when time constant of detector is not selected properly. If the modulating voltage is faster than the rate of voltage fall across RC combination resulting in distorted output. This type of distortion is called diagonal clipping which results in distorted output.



Fig 1.18 Diagonal Clipping

To avoid the diagonal clipping proper value of RC needs to be selected. The voltage across RC combination during the non-conducting period of diode is Vc at an instant t which is given by

$$V_C(t) = V_0 e^{-\frac{t}{RC}}$$

The rate of slope in capacitor due to period discharging is calculated by differentiating  $V_C(t)$  So

$$\frac{dV_C(t)}{dt} = \frac{dV_C}{dt} = \frac{-V_0 e^{-\frac{t}{RC}}}{RC} = \frac{-V_C(t)}{RC}.$$
(1)

The decrease in capacitor voltage must follow the modulation envelope if distortion is to be avoided. The envelope of the modulated voltage is given by

$$e_{AM} = E_C \left( 1 + m_a \cos \omega_m t \right)$$

The slope of the envelope is given by

$$\frac{de_{AM}}{dt} = \frac{d}{dt} \left[ E_C \left( 1 + m_a \cos \omega_m t \right) \right]$$
$$= -m_a E_C \omega_m \sin \omega_m t \qquad ------(2)$$

To avoid the clipping the slope of capacitor voltage  $V_C$  should be algebraically equal or less than the slope of envelope voltage, so

$$-\frac{V_{C}(t)}{RC} \leq -E_{C}m_{a}\omega_{m}\sin\omega_{m}t$$
$$\frac{V_{C}(t)}{RC} \geq E_{C}m_{a}\omega_{m}\sin\omega_{m}t$$
$$\frac{E_{C}(1+m_{a}\cos\omega_{m}t)}{RC} \geq E_{C}m_{a}\omega_{m}\sin\omega_{m}t$$

Mathematically the above equation is written as

$$\frac{1}{RC} \ge \frac{m_a \omega_m \sin \omega_m t}{\left(1 + m_a \cos \omega_m t\right)}$$
 ------(3)

To find the maximum amount of RC differentiate the equation 3 and equate it to zero

$$\frac{d}{dt}\frac{m_a\omega_m\sin\omega_m t}{\left(1+m_a\cos\omega_m t\right)}=0$$

$$m_a \omega_m \frac{\left(1 + m_a \cos \omega_m t\right) \cos \omega_m t \omega_m - \sin \omega_m t}{\left(1 + m_a \cos \omega_m t\right)} \frac{m_a (-\sin \omega_m t) \omega_m}{m_a - \sin \omega_m t} = 0$$

 $\omega_m \cos \omega_m t + (m_a \cos^2 \omega_m t)\omega_m + (m_a \sin^2 \omega_m t)\omega_m = 0$ 

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 $\omega_{\rm m} \cos \omega_{\rm m} t + m_{\rm a} \omega_{\rm m} (\cos^2 \omega_{\rm m} t + \sin^2 \omega_{\rm m} t) = 0$ 

$$\omega_{\rm m} \cos \omega_{\rm m} t + m_{\rm a} \omega_{\rm m} = 0$$

on substituting the value of  $\cos \omega_m t$  in  $\cos^2 \omega_m t + \sin^2 \omega_m t = 1$  we get  $\sin \omega_m t = \sqrt{1 - m_a^2}$  -----(5)

substituting equation 4 and 5 in 3 we get 
$$\frac{1}{RC} \ge \frac{m_a \omega_m \sqrt{1 - ma2}}{1 - m_a^2}$$

By simplifying 
$$RC \ge \frac{\sqrt{1-m_a^2}}{m_a \omega_m}$$

So RC depends on the  $m_a$  value. So the RC to be selected by satisfying the condition in order to avoid distortion and the modulation index value should be correct, if it is large then it will provide negative peak clipping. So the envelope detector will be changed for smooth functioning by attaching a  $\pi$  section low pass filter at the output.

### **Negative peak clipping**:

- > The  $2^{nd}$  source of distortion in linear diode detector is the curvatures of the diode characteristics. So as a result the efficiency varies. It will be reduced by selecting load resistance value large. So when  $R_C$  is large then  $m_a$  will be low and signal becomes clipped at the negative peaks.
- > The negative peak clipping provides ac and dc load impedances unequal.

### **DOUBLE SIDEBAND SUPPRESSED CARRIER (DSBSC) MODULATION**

In AM with carrier scheme, there is wastage in both transmitted power and bandwidth. In order to save the power in amplitude modulation the carrier is suppressed because it does not contain any useful information. This scheme is called as the double side band suppressed carrier amplitude Modulation (DSB-SC). It contains LSB and USB terms, resulting in a transmission bandwidth that is twice the bandwidth of the message signal.

Let us consider the message and carrier signal as,

 $e_{m}(t) = E_{m} \sin \omega_{m} t -----(1)$  $e_{c}(t) = Ec \sin \omega_{c} t -----(2)$ 

For obtaining the DSB-SC wave multiply both carrier signal and message signal hence,

 $e(t)_{DSB-SC} = e_{m}(t).e_{c}(t)$   $=Em.Ec \ sin\omega_{m} t \ sin\omega_{c} t$   $e(t)_{DSB-SC} = Em.Ec \ [ \ cos(\omega_{c} - \omega_{m})t - cos(\omega_{c} + \omega_{m})t ]$  2 USB LSB

From this equation we know that the carrier is suppressed in double side band suppressed carrier.

Graphical Representation of DSB-SC AM:



Fig 1.19 (a) Baseband signal (b) DSBSC







It shows that carrier term  $\omega_c$  is suppressed. It contains only two sideband terms having frequency ( $\omega_c - \omega_m$ ) and ( $\omega_c + \omega_m$ ). Hence this scheme is called as DSB-SC AM.

Phasor representation of DSB-SC AM:



The total power transmitted in AM is  $P_t = P_{carrier} + P_{LSB} + P_{USB}$ 

If the carrier is suppressed, then the total power transmitted is

$$P_t' = P_{LSB} + P_{USB}$$

We know that,  $P_{LSB} = P_{USB} = \frac{m_a^2 Ec^2}{8R}$  $P_t' = m_a^2 Ec^2 + \frac{m_a^2 Ec^2}{8R}$  $= m_a^2 Ec^2 = m_a^2 Pc$ 4R = 2

Therefore the power saving with respect to AM is

Power Saving = 
$$\frac{P_t - P_t}{P_t}$$
 x 100  
=  $[1 + m_a^2/2] P_C - [m_a^2/2] P_C$   
 $[1 + m_a^2/2] P_C$   
=  $\frac{P_C}{[1 + m_a^2/2] P_C}$ 

% Power Saving = 
$$\frac{2}{2+m_a^2} \times \frac{100}{2}$$

If  $m_a = 1$ , then power saving (2/3) x 100 = 66.7 % i.e 66.7% of power is saved by using DSB-SC-AM.

### **Advantages**

DSB-SC is more efficient in transmitted power as compared to DSB-FC. DSB-FC hs better signal to noise ratio as compared to SSB transmission.

### **Disadvantages**

Bandwidth remains same as DSB-FC even though the carrier is suppressed.

# **GENERATION OF AM-DSBSC**

- 1. Balanced Modulator Method
- 2. Ring Modulator Method

# **BALANCE MODULATOR METHOD**

> The same circuit can be used to generate AM with carrier. The main difference between AM with

carrier generation and DSB-SC –AM is the feeding points of the carrier and modulating signals are interchanged.

- The transistor is operated in a balanced mode thus heavy filtering is not required to remove the unwanted harmonics.
- It is assumed that the two transistors are identical and the circuit is symmetrical. The operation is confined in the nonlinear region of the active devices employed in this circuit. The carrier voltages across the upper and lower part of the secondary windings of the center tap transformers are equal in magnitude and opposite in phase.



Fig 1.22 Balanced Modulator for DSB-SC AM Generation

# Principle of operation:

- > The modulating signal is applied as the input to the transistor  $T_1$  and  $T_2$  and the carrier signal is applied to the common input of the push pull amplifier configuration. Because of centre tap transformers are equal and opposite in phase  $V_m = -V_m$
- Input to the transistor T1 is given by,

$$V_{be} = e_m(t) + e_c(t)$$

 $V_{be} = E_m \sin \omega_m t + E_c \sin \omega_c t$ (1)

Similarly Input to the transistor T2,

 $V'_{be} = -e_m(t) + e_c(t)$   $V'_{be} = -E_m \sin\omega_m t + E_c \sin\omega_c t \qquad ------(2)$ By using the non-linearity property the collector current can be written as per square law equation  $i_c = a_1 V_{be} + a_2 V_{be}^2 + \dots + a_2$ 

On substituting eqn 3 and 4 in 1 and 2 we get

 $i_c = a_1 [E_m \sin \omega_m t + E_c \sin \omega_c t] + a_2 [E_m \sin \omega_m t + E_c \sin \omega_c t]^2$ 

 $i_c = a_1 \left[ E_m \sin \omega_m t + E_c \sin \omega_c t \right] + a_2 E_m^2 \sin^2 \omega_m t + a_2 E_c \sin^2 \omega_c t + 2a_2 E_m E_c \sin \omega_m t \sin \omega_c t - \dots - (5)$ 

# Similarly

 $i_c = a_1 \left[ -E_m \sin \omega_m t + E_c \sin \omega_c t \right] + a_2 \left[ -E_m \sin \omega_m t + E_c \sin \omega_c t \right]^2$ 

 $i_c = a_1 \left[ -E_m \sin \omega_m t + E_c \sin \omega_c t \right] + a_2 E_m^2 \sin^2 \omega_m t + a_2 E_c^2 \cos^2 \omega_c t - 2a_2 E_m E_c \sin \omega_m t \sin \omega_c t - \dots - (6)$ 

The output AM voltage  $V_0$  is given by  $V_0 = K[i_c - i'_c]$  -----(7)

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Because  $i_{c_1}$  i'<sub>c</sub> flows in the opposite direction and 'K' is a constant depending on impedance or other circuit parameters.

On substituting equation 5 and 6 in 7 we get,

$$\begin{split} V_{o} &= K[\ i_{c} - i'_{c}\ ] \\ V_{o} &= K\ [2a_{1}\ Em\ sin \omega_{m}t + 4a_{2}\ Em\ Ec\ sin \omega_{m}t\ sin \omega_{c}t] \end{split}$$

The output contains the original modulating signal and the two sidebands. The modulating signal has been suppressed by tuning the tank circuit to the center frequency  $\pm \omega_c$ 

 $V_{o} = 4Ka_{2} \text{ Em Ec } \sin\omega_{m}t \sin\omega_{c}t$ = 2Ka\_{2} Em Ec[ cos(\omega\_{c} - \omega\_{m})t - cos(\omega\_{c} + \omega\_{m})t]

- So only the side bands are present in the o/p. Hence the DSB-SC-AM generated.
- The main advantage of this modulator is saving power and efficiency because of the suppressing of the carrier.

# **RING MODULATOR METHOD**

- The balanced Ring modulator circuit is widely used in carrier telephony suppresses both unwanted modulating and carrier signal in its output.
- > Ring modulator is a type of product modulator which is used to generate DSB-SC Signal.
- The band pass filter is not used at the output hence the harmonic frequencies are automatically controlled.
- In a ring modulator circuit four diode are connected in the form of ring in which all the four diodes are connected in the same manner and are controlled by a square wave carrier signal e<sub>c</sub> (t).
- The carrier signal acts as a switching signal to alternate the polarity of the modulating signal at the carrier frequency.
- > When no modulating signal is present diode  $D_1$  and  $D_2$  or  $D_3$  and  $D_4$  will conduct depending upon polarity of the carrier.

# **POSITIVE HALF CYCLE OF CARRIER:**

- > Diodes  $D_1$  and  $D_3$  are forward biased. At this time  $D_2$  and  $D_4$  are reverse biased and act like open circuits. The current divides equally in the upper and lower portion of the primary winding T2.
- The current in the upper part of the winding produces a magnetic field that is equal and opposite to the magnetic field produced by the current in the lower half of the secondary.
- Therefore the magnetic fields cancel each other out and no output is induced in the secondary. Thus the carrier is effectively suppressed.

# **NEGATIVE HALF CYCLE OF CARRIER:**

- When the polarity of the carrier reverses. Diodes D<sub>1</sub> and D<sub>2</sub> are reverse biased and the diodes D<sub>3</sub> and D<sub>4</sub> will conduct. Again the current flows in the secondary winding of T1 and the primary winding of T2.
- The equal and opposite magnetic fields produced in T2 cancel each other and thus result in zero carrier output. The carrier is effectively balanced out.

# PRINCIPLE OF OPERATION

- When both the carrier and the modulating signals are present, during positive half cycle of the carrier diodes D<sub>1</sub> and D<sub>2</sub> conduct, while diodes D<sub>3</sub> and D<sub>4</sub> does not conduct.
- During negative half cycle of the carrier voltage diodes D<sub>3</sub> and D<sub>4</sub> conduct and D<sub>1</sub> and D<sub>2</sub> does not conduct.
- When polarity of the modulating signal changes the result is a 180 phase reversal. At the time D<sub>3</sub> and D<sub>4</sub> are in forward bias.

Let us consider the modulating voltage,

$$e_{m}(t) = E_{m} \sin \omega_{m} t \qquad -----(1)$$

$$e_{c}(t) = E_{c} \sin \omega_{c} t \qquad -----(2)$$
The output voltage is  $V_{0}(t) = e_{m}(t).e_{c}(t)$ 

$$= E_{m}.E_{c} \sin \omega_{m} t \sin \omega_{c} t$$

$$V_{0}(t) = E_{\underline{m}}\underline{E}_{c} [\cos(\omega_{c} - \omega_{m})t - \cos(\omega_{c} + \omega_{m})t] \qquad -----(3)$$

$$\frac{1}{2}$$

$$LSB \qquad USB$$

The equation 3 shows that the o/p is free from the carrier and other higher order terms and it contains upper and lower sidebands only. The ring modulator circuit is also known as double balanced modulator because it is balanced with respect to both the baseband signal and the square wave carrier. The main advantage is the o/p is stable and long life, no external source to activate the diodes.



Fig 1.23 Ring Modulator and Waveform

# DEMODULATION/DETECTION OF AM-DSBSC

Coherent Detector Non Coherent Detector

### SYNCHRONOUS OR COHERENT DETECTOR

The coherent detector uses exact carrier synchronization for retrieving the message signal from modulated signal. These types of detectors are mainly used for detecting DSB&SSB signals.

- > It consists of a product modulator with a low pass filter.
- For detecting signal local oscillator at the receiver end is required. The frequency and phase of the locally generated carrier and transmitter carrier must be synchronized that is exactly coherent.
- All types of linear modulation can be detected by using synchronous detector. It consists of a product modulator with LPF.



### **Fig 1.24 Coherent Detector**

- > The incoming signal is first multiplied with locally generated carrier and then passed through low pass filter. The filter bandwidth is same as the message bandwidth  $\omega_m$
- > The local oscillator should be exactly synchronized with carrier signal in both phase and velocity.
- > Considering the case of DSB-SC signal, the signal I/p is

 $e_1(t) = E_m \cdot Ec \sin \omega_m t \sin \omega_c t$  $e_2(t) = E \sin \omega_c t$ 

The output of the non linear device which acts as a multiplying device is given by

 $e(t)=e_1(t)$ .  $e_2(t)=E_m.E_c E \sin \omega_m t \sin^2 \omega_c t$ 

$$e(t) = E_m \cdot E_c \operatorname{Esin} \omega_m t \left( \frac{1 - \cos 2\omega_c t}{2} \right)$$

After passing through the LPF the second order harmonic term is eliminated.

$$e(t) = \underline{E_m \cdot E_c \cdot Esin\omega_m t}{2}$$

Assume the local oscillator carrier to have a phase difference with the transmitted carrier. The carrier is represented by

$$e_2(t) = Esin(\omega_c t + \varphi)$$

The output of the non linear device is given by

 $e(t) = e_1(t)$ .  $e_2(t) = E_m$ . Ec E sin $\omega_m t$  sin $\omega_c t$  sin ( $\omega_c t + \varphi$ )

 $= E_m E_c E \sin \omega_m t \sin \omega_c t [\sin \omega_c t \cos \varphi + \cos \omega_c t \sin \varphi]$ 

 $= E_m \cdot E_c E \sin \omega_m t \sin^2 \omega_c t \cos \varphi + E_m \cdot E_c E \sin \omega_m t \sin \omega_c t \cos \omega_c t \sin \varphi$ 

$$= E_{m}.E_{c} E \sin \omega_{m} t \cos \varphi \quad \left(\frac{1 - \cos 2\omega_{c} t}{2}\right) + E_{m}.E_{c} E \sin \omega_{m} t \sin \omega_{c} t \cos \omega_{c} t \sin \varphi$$

$$= \underline{E_m.E_c E \sin\omega_m t \cos\varphi} - \underline{E_m.E_c E \sin\omega_m t \cos\varphi \cos2\omega_c t} + E_m.E_c E \sin\omega_m t \sin\omega_c t \cos\omega_c t \sin\varphi}_2$$

After passing through the LPF the second order harmonic term is eliminated.

$$e(t) = \underline{E_m.E_c} \underline{Esin\omega_m t} \underline{cos\phi}$$

$$2$$
If  $\phi = 0$  then  $e(t)$  is maximum  $e(t) = \underline{E_m.E_c} \underline{Esin\omega_m t}$ 
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$$3$$
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If  $\phi = 90$  then e(t) is minimum e(t) = 0

The demodulated signal  $V_o(t)$  is therefore proportional to the message signal when the phase error,  $\varphi = 0$  and it is minimum (zero) when  $\varphi = \pm \frac{\pi}{2}$ . Thus the phase error  $\varphi$  in the local oscillator causes the detector output to be attenuated by a factor equal to  $\cos\varphi$ . As long as the phase error is constant, the detector provides an undistorted version of the original baseband signal.

### **COSTAS PLL DETECTOR**



### Fig 1.25 Costas PLL Detector

- Costas receiver is one of the method for obtaining a practical synchronous receiver suitable for demodulating DSB-SC waves. It consists of two coherent detectors supplied with the same input signal.
- One detector is supplied with the DSB-SC AM and locally generated carrier which is in phase with the transmitted carrier. This detector is known as "In-phase coherent detector or I channel".
- The other detector is supplied with the DSB-SC AM and locally generated carrier which is quadrature phase with the transmitted carrier. This detector is known as "Quadrature coherent detector or Q channel".
- These two detectors are coupled together to form a negative feedback system designed in such a way as to maintain the local oscillator synchronous with the carrier wave.

### **Operation of the circuit**:

- In this case I channel output contains the desired demodulated signal where as Q channel output is zero due to the quadrature null effect of Q channel.
- Suppose there is some phase shift  $\phi$  radians between local oscillator carrier and the transmitting carrier then I channel output will remain essentially unchanged. But Q channel output contains some signal which is proportional to sin  $\phi$
- This Q channel output will have same polarity as the I channel output for one direction of local oscillator whereas the polarity will be opposite to the I channel for the other direction of phase shift.
- Thus the I and Q channel outputs are combined in phase discriminator
- The phase discriminator provides a d.c. control signal which may be used to correct local oscillator phase error.
- The local oscillator is a voltage controlled oscillator. Its frequency can be adjusted by an error control d.c signal.
- The costas receiver ceases phase control when there is no modulation and that phase lock has to be reestablished with reappearance of modulation.

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# SINGLE SIDEBAND SUPPRESSED CARRIER

In AM with carrier both the transmitting power and bandwidth is wasted. Hence the DSB-SC AM scheme has been introduced in which power is saved by suppressing the carrier component but the bandwidth remains same.

- Increase in the saving of power is possible by eliminating one sideband in addition to the carrier component because the USB and LSB are uniquely related by symmetry about the carrier frequency. So either one sideband is enough for transmitting as well as recovering the useful message. The block diagram of SSB-SC AM is shown in figure.
- As for as transmission information is concerned only one side band is necessary. So if the carrier and one of the two sidebands are suppressed at the transmitter, no information is lost.
- This type of modulation is called as single side band suppressed carrier-AM and the SSB system reduces the band width by half.



Block diagram of SSB-SC AM is shown in figure.

# Fig 1.26 SSB-SC AM Modulator

- The single side band suppressed carrier can be obtained as follows,
- In order to suppress one of the sideband, the input signal fed to the modulator1 is 90° out of phase with that of the signal fed to the modulator'2'.

Let 
$$e_1(t) = E_m \cos \omega_m t \cdot E_c \cos \omega_c t$$

$$e_2(t) = E_m \sin \omega_m t$$
 . $E_c \sin \omega_c t$ 

Therefore,  $e(t)_{SSB} = e_1(t) + e_2(t)$ 

$$= E_m E_c [\cos \omega_m t. \cos \omega_c t + \sin \omega_m t. \sin \omega_c t]$$

$$e(t)_{SSB} = E_m E_c \cos (\omega_c - \omega_m) t.$$

We know that for DSB-SC AM

$$e_{\text{DSB-SC}}(t) = E_{\underline{m}} \underline{Ec} \left[ \cos(\omega_c + \omega_m)t + \cos(\omega_c - \omega_m)t \right]$$

When comparing equations of  $e(t)_{SSB-SC}$  and  $e_{DSB-SC}(t)$ , one of the sideband is suppressed. Hence this scheme is known as SSB-SC AM.



FIg 1.27 Frequency Spectrum Of SSB-SC-AM:

• The Frequency spectrum shows that only one side band signal is present, the carrier and the other sideband signal are suppressed. Thus the bandwidth required reduces from 2  $\omega_m$  to  $\omega_m$  i.e., bandwidth requirement is reduced to half compared to AM & DSB-SC signals.

### Phasor representation of SSB-SC-AM:



### Power calculation: Fig 1.28 Phasor diagram of SSB-SC AM

Power in sidebands  $P_t$ " =  $P_{LSB} = P_{USB} = m_a^2 V_c^2 / 8R = m_a^2 Pc / 4$ Power saving with respect to AM with carrier Power saving =  $P_t - P_t$ "x100  $P_t$ 

where  $P_t$  = Total power transmitted.

Power saving = 
$$[1 + m_a^2/2] P_C - [m_a^2/4] P_C$$
 =  $P_C + [m_a^2/2] P_C - [m_a^2/4] P_C$   
 $[1 + m_a^2/2] P_C$   
 $\frac{1 + \frac{m_a^2}{4}}{1 + \frac{m_a^2}{2}} \times 100$   
 $= \frac{\frac{4 + m_a^2}{4}}{\frac{2 + m_a^2}{2}} \times 100$   
 $= \frac{4 + m_a^2}{4 + 2m_a^2} \times 100$ 

If  $m_a=1$  then % power saving= (5/6) x100=83.3% So we can save 83.3% of power with respect to AM with carrier.

We can also find the power in SSB-SC-AM with respect to AM with DSB-SC system,

$$powersaving = \frac{p_{t}' - p_{t}''}{p_{t}'} \times 100$$
$$= \frac{\frac{m_{a}^{2} P_{c}}{2} - \frac{m_{a}^{2} P_{c}}{4}}{\frac{m_{a}^{2} P_{c}}{2}} \times 100$$

If m<sub>a</sub>=1 then % power saving=50%.therefore 50% power is saved with respect to DSB-SC System.

### **Applications of SSB**

- 1. Used to save applications where such a power saving is warranted, i.e., in mobile system, in which weight and power consumption must naturally be kept low.
- 2. Single sideband modulation is at a premium. Point-to-Point communication, land, air, maritime mobile communication, TV, Telemetry, Military and Radio navigation are the greatest use of SSB in one form or another.

### SSB Advantages

- *Power conservation*: Much less total transmitted power required to produce the same quality signal.
- Bandwidth conservation: Half of the bandwidth of conventional AM bandwidth.
- Selective Fading: Not present in SSBSC.
- *Noise Reduction:* Since SSB uses half the bandwidth, the thermal noise power is reduced to half. Hence immunity to selective fading is improved.

### SSB Disadvantages

- *Complex Receivers:* Required carrier recovery and synchronization circuit adds cost, complexity and size.
- Tuning Difficulties: Complex and Expensive Tuning Circuits.

# **GENERATION OF SSB**

- 1. Filter Method
- 2. Phase Shift Method
- 3. Modified Phase Shift Method or Weaver Method

# FILTER METHOD



Fig 1.29 Filter Method of SSB Generation

In this method of SSB generation, after the BM, the unwanted sideband is removed (actually heavily attenuated) by a filter and hence this name. The filter may be LC, ceramic or mechanical depending upon

the carrier frequency and other requirements. Such a filter must have a flat bandpass and extremely high attenuation outside the passband.

In radio communication system, the frequency range used for voice is 300 Hz to about 2800 Hz in most cases. If it is required to suppress the lower sideband and if the transmitting frequency is  $f_c$ , then the lowest frequency that this filter must pass without attenuation is  $f_c+300$  Hz whereas the highest frequency that must be fully attenuated is  $f_c-300$  Hz. So we need a filter whose transition band is very low. This situation becomes worse if lower modulating frequencies are employed, such as the 50 Hz minimum in AM broadcasting. In order to obtain a filter response curve with skirts as steep the 'Q' of the tuned circuits must be very high.

The initial modulation takes place in the balanced modulator at a low frequency (such as 100 kHz) because of the difficulty of making adequate filters at higher frequencies. The filter is a BPF with a sharp cutoff frequency at either side of the bandpass to obtain satisfactory adjacent sideband rejection. The filtered signal is up-converted in a mixer to the final transmitter frequency and then amplified before being coupled to the antenna. The integrated ceramic filters are used as sideband filters. The drawback of filter method is that it requires sharp filtering, which requires filters with high Q. Primary modulation cannot be done at the transmitting frequency which is another drawback of the filter method.

# PHASE SHIFT METHOD

- This method avoids the prime disadvantage of filtering method. That is requirement of a sideband filter with a narrow transition band and it cannot be used for very low and very high frequencies.
- This method does not have any sideband filters and the primary modulation can be done at the transmitting frequency. The unwanted sideband can be removed by generating the components of sideband out of phase.
- If the undesired sideband is LSB then the two LSB are generated such that they are 180 out of phase with each other. So that USB add with each other and LSB cancel each other. When two undesired sideband components are added they cancel each other with only the presence of desired signal.
- Two balanced modulators and two phase shifters are used. One of the modulator BBM1 receives the carrier voltage shifted by 90° and the modulating voltage, where as another balanced modulator BBM2 receives the modulating voltage shifted by 90° and the carrier voltage.
- The carrier signal is cancelled out by both the balanced modulator and then unwanted sidebands cancel at the output of the summing amplifiers and hence produces SSB signal.



Fig 1.30 Phase shift Method

### Mathematical analysis:

For modulator1 (BM1)  $e_{c}(t) = E_{c} \sin(\omega_{c} t + 90^{0}) = E_{c} \cos\omega_{c} t$   $e_{m}(t) = E_{m} \sin\omega_{m} t$ For modulator2(BM2)  $e_{c}(t) = E_{c} \sin\omega_{c} t$   $e_{m}(t) = E_{m} \sin(\omega_{m} t + 90^{0}) = E_{m} \cos\omega_{m} t$ Output for modulator(BM1)isV<sub>1</sub>  $V_{1} = E_{c} \cos\omega_{c} t E_{m} \sin\omega_{m} t \qquad -----(1)$ Output for modulator(BM2)isV<sub>2</sub>  $V_{2} = E_{c} \sin\omega_{c} t. E_{m} \cos\omega_{m} t \qquad -----(2)$ 

The output of adder is

Thus one of the side band is cancelled where as the other is reinforced. This method avoids the use of filters.

# MODIFIED PHASE SHIFT METHOD (OR) WEAVER'S METHOD

- The modified phase shift method overcomes the limitation of phase shift method. That is AF phase shift network is required to operate over a large range of audio frequencies but also retains the advantage like its ability to generate SSB at any frequency and use of low audio frequency.
- This method provides both RF and AF oscillator phase shift and also used in low frequency and so it can be used for both audio and radio frequencies.



Fig 1.31 Modified Phase shift Method

# WEAVER'S METHOD

- Modulators 1 and 2 both have the unshifted modulating signal as inputs. BM1 takes low frequency subcarrier with a 90 phase shift from the AF oscillator. BM2 receives the subcarrier signal directly from the oscillator.
- This method tries to aEoid the phase shift of audio frequencies and combine the audio frequency carrier with AF which lies in the middle of audio frequency.
- The low pass filter at the output of BM1 and BM2 with cut off frequency ensures the input to the balance modulator BM3 and BM4. The output of BM3 and BM4 gives the desired sideband suppression.

# MATHEMATICAL ANALYSIS

The modulating signal is	$em = Em \sin \omega_m t$	(1)
The A.F carrier(sub carrier signal)	$eo(t) = 2E_0 \sin\omega_0 t$	(2)
The R.F carrier	$ec(t)=2Ec \sin\omega_c t$	(3)

The input for Balanced modulator 1(BM1) is  $em(t) = Em \sin\omega_m t$  $eo(t) = 2E_0 \sin(\omega_0 t + 90^0)$ 

The output for Balanced modulator 1(BM1) is  $e1 = Em \sin\omega_m t \ 2E_0 \sin (\omega_0 t + 90^0)$   $= Em \ E_0 \left[ \cos(\omega_0 t + 90^0 - \omega_m t) - \cos(\omega_0 t + 90^0 + \omega_m t) \right]$ ------(4)

The input for Balanced modulator 2(BM2) is  $em(t) = Em \sin\omega_m t$  $eo(t) = 2E_0 \sin\omega_0 t$ 

```
The output for Balanced modulator 2(BM2) is

e2 = Em \sin\omega_m t 2E_0 \sin\omega_0 t
= Em E_0 [\cos(\omega_0 t - \omega_m t) - \cos(\omega_0 t + \omega_m t)] \qquad -----(5)
```

The LPF1, 2 eliminates the upper sidebands of the modulator. Hence USB is suppressed

The Output of LPF1 is $e3 = Em E_0 [\cos(\omega_0 t + 90^0 - \omega_m t)]$	(6)

The Output of LPF2 is  $e4 = Em E_0 \cos(\omega_0 t - \omega_m t)$  -----(7)

The output of LPF1, 2 are given to BM3, BM4.

The input for Balanced modulator 3(BM3) is  $e3= Em E_0 [\cos(\omega_0 t+90^0 - \omega_m t) + ec(t) = 2Ec \sin\omega_c t$ 

The output for Balanced modulator 3(BM3) is  $e5 = 2Em E_0 Ec \cos(\omega_0 t+90^0 - \omega_m t) \sin\omega_c t$ 

Assume  $Em = E_0 = Ec = 1$ , then  $e5 = 2\cos(\omega_0 t + 90^0 - \omega_m t) \sin\omega_c t$   $=\sin[(\omega_{c} + \omega_{o} - \omega_{m})t + 90^{0}] + \sin[(\omega_{c} - \omega_{0} + \omega_{m})t - 90^{0}] - \dots - (8)$ 

The input for Balanced modulator 4(BM4) is  $e4= Em E_0 \cos(\omega_0 t - \omega_m t)$  $ec(t) = 2Ec \sin(\omega_c t+90^0)$ 

The output for Balanced modulator 4(BM4) is  $e6 = Em E_0 \cos(\omega_0 t - \omega_m t) 2Ec \sin(\omega_c t + 90^0)$ Assume  $Em = E_0 = Ec = 1$ , then  $e6 = 2 \cos(\omega_0 t - \omega_m t) \sin(\omega_c t + 90^0)$   $= \sin[(\omega_c + \omega_0 - \omega_m)t + 90^0] + \sin[(\omega_c - \omega_0 + \omega_m)t + 90^0] -----(9)$ 

The output of adder is 
$$e_{SSB-SC}(t) = e5 + e6$$

 $= \sin[(\omega_{c} + \omega_{o} - \omega_{m})t + 90^{0}] + \sin[(\omega_{c} - \omega_{0} + \omega_{m})t - 90^{0}] + \\ \sin[(\omega_{c} + \omega_{o} - \omega_{m})t + 90^{0}] + \sin[(\omega_{c} - \omega_{0} + \omega_{m})t + 90^{0}]$ 

$$=2 \sin[(\omega_0 + \omega_c - \omega_m)t + 90^0]$$

The other two terms cancel with each other because it is out of phase.

$$e_{SSB-SC}(t) = 2\cos[(\omega_0 + \omega_c - \omega_m)]t$$

The final RF output frequency is  $\omega_0 + \omega_c - \omega_m$  which is essentially the lower side band of RF carrier  $\omega_0 + \omega_c$ .

### DEMODULATION/DETECTION OF AM-SSBSC

### SYNCHRONOUS OR COHERENT DETECTOR

- The coherent detector uses exact carrier synchronization for retrieving the message signal from modulated signal. These types of detectors are mainly used for detecting DSB&SSB signals.
- > It consists of a product modulator with a low pass filter.
- For detecting signal local oscillator at the receiver end is required. The frequency and phase of the locally generated carrier and transmitter carrier must be synchronized that is exactly coherent.
- All types of linear modulation can be detected by using synchronous detector. It consists of a product modulator with LPF.



### **Fig 1.32 Coherent Detector**

- > The incoming signal is first multiplied with locally generated carrier and then passed through low pass filter. The filter bandwidth is same as the message bandwidth  $\omega_m$
- > Tthe local oscillator should be exactly synchronized with carrier signal in both phase and velocity.
- > Considering the case of SSB-SC signal, the signal I/p is

$$e_{1}(t) = \underline{E_{m} \cdot E_{c} \cos (\omega_{c} - \omega_{m})t}{2}$$
$$e_{2}(t) = E \sin \omega_{c} t$$

The output of the non linear device which acts as a multiplying device is given by

$$e(t) = e_{1}(t). e_{2}(t) = \underline{E}_{m}.\underline{E}_{c} \underline{E} \cos (\omega_{c} - \omega_{m})t \sin \omega_{c} t$$

$$2$$

$$e(t) = \underline{E}_{m}.\underline{E}_{c} \underline{E} \left( \underline{\sin \omega_{m} t} + \underline{\sin (2\omega_{c} - \omega_{m})t} \right)$$

2 The first term of the output is the modulating frequency signal that is passed on to the output. The second component is a RF component and is attenuated by the filter. Thus the synchronous detector is capable of demodulating SSB-SC signal

$$e(t) = \underline{E_m \cdot E_c \ Esin \omega_m t}{4}$$

2

The synchronous detector is effective only when locally generated carrier is properly synchronize with the transmitter power. Assume the local oscillator carrier to have a phase difference with the transmitted carrier. The carrier is represented by

$$e_2(t)=Esin(\omega_c t + \phi)$$

The output of the non linear device is given by

$$e(t) = e_{1}(t). e_{2}(t) = \underline{E_{m}.E_{c} \cos (\omega_{c} - \omega_{m})t}$$
 Esin (  $\omega_{c} t + \varphi$  )  

$$= \underline{E_{m}.E_{c} E} \cos (\omega_{c} - \omega_{m})t \sin (\omega_{c} t + \varphi)$$

$$= \underline{E_{m}.E_{c} E} (\cos\omega_{c} t \cos\omega_{m}t + \sin\omega_{m}t \sin \omega_{c}t)(\sin\omega_{c} t \cos\varphi + \cos\omega_{c} t \sin\varphi)$$

$$2$$

$$= \underline{E_{m}} \cdot \underline{E_{c}} \underline{E} \left[ \cos \omega_{c} t \cos \omega_{m} t \sin \omega_{c} t \cos \phi + \sin \omega_{m} t \sin^{2} \omega_{c} t \cos \phi + 2 \cos^{2} \omega_{c} t \cos \omega_{m} t \sin \phi + \cos \omega_{c} t \sin \omega_{c} t \cos \omega_{m} t \cos \phi \right]$$

$$= \underline{E_{m} \cdot E_{c} \cdot E} \left[ \cos \omega_{c} t \cos \omega_{m} t \sin \omega_{c} t \cos \varphi + \sin \omega_{m} t \cos \varphi \left( \frac{1 - \cos 2\omega_{c} t}{2} \right) \right]$$

$$Cos^{2} \omega_{c} t \cos \omega_{m} t \sin \varphi + \cos \omega_{c} t \sin \omega_{c} t \cos \omega_{m} t \cos \varphi \right]$$

After passing through the LPF the second order harmonic term is eliminated.

$$e(t) = \underline{E}_{\underline{m}} \cdot \underline{E}_{\underline{c}} \cdot \underline{E} \sin \omega_{\underline{m}} t \cdot \cos \varphi_{\underline{a}}$$

If  $\varphi = 0$  then e(t) is maximum  $e(t) = \underline{E}_m . \underline{E}_c \underline{E} sin \omega_m t$ 4

If  $\varphi = 90$  then e(t) is minimum e(t) = 0

Thus there is a phase delay due to improper synchronization.

### VESTIGEAL SIDE BAND MODULATION

Definition : One of the sideband is partially suppressed and vestige (portion) of the other sideband is transmitted, This vestige (portion) compensates the suppression of the sideband. It is called vestigial sideband transmission.

### Generation and demodulation of VSB

A VSB signal is obtained as shown figure below by  $\sup pressing$  one of the sidebands of a DSBSC using a VSB filter.



### Fig 1.33 VSB Generation and Demodulation

VSB filter is a BPF having an asymmetric frequency response in the transition band, positioned in such a way that the carrier frequency corresponds to the middle of the transition band. From the figure,

$$S_{DSB-SC}(t) = A_c m(t) cos(\omega_c t)$$

The transfer function of the VSB filter is  $H_{\nu}(\omega)$ .



### Fig 1.34 Transfer Function of VSB

The inverse FT of  $H_v(\omega)$  gives the unit impulse,  $h_v(t)$ . We can express the VSB filter output as:  $S_{VSB-SC}(t) = S_{DSB-SC}(t) * h_v(t) = A_c m(t) cos(\omega_c t) * h_v(t)$  ------(1) Taking FT on both sides,

$$S_{VSB-SC}(\omega) = \left\{ \frac{A_c}{2} [M(\omega - \omega_c) + M(\omega + \omega_c)] \times H_{\nu}(\omega) \right\} \qquad -----(2)$$

The coherent detector is a sort of universal detector of AM signals in the sense that DSBSC, conventional AM and SSBSC can all be detected successfully by using it. It would be natural to expect that coherent detection to work for the VSB-SC signal too.



#### Fig 1.35 VSB Demodulator

The output of the multiplier in the VSB demodulator in the figure is given by:

$$x(t) = S_{VSB-SC}(t) \times A_0 cos(\omega_c t) \qquad ------$$

It is assumed perfect synchrony between the transmitter and demodulator carriers.

Taking FT on both sides of equation (3), we obtain,

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(3)

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Using (2) in (4),

$$X(\omega) = \left(\frac{A_0 A_c}{4}\right) \{ [M(\omega) + M(\omega - 2\omega_c)] H_v(\omega - \omega_c) + [M(\omega + 2\omega_c) + M(\omega)] H_v(\omega + \omega_c) \}$$

The signal x(t) is passed through an ideal filter (LPF) to obtain y(t). If the VSB modulation is successful, then y(t) should be proportional to the message signal, m(t).

It is observed from (5) that  $M(\omega - 2\omega_c)$  and  $M(\omega + 2\omega_c)$  are high pass terms, since they represent  $M(\omega)$  translated by  $\pm 2\omega_c$ . These terms are blocked by the LPF which yields an output signal y(t) with the FT  $Y(\omega)$  given by

$$Y(\omega) = \left(\frac{A_0 A_c}{4}\right) M(\omega) [H_v(\omega - \omega_c) + H_v(\omega + \omega_c)]$$
 -----(6)

VSBSC modulation and demodulation is considered to be successful if  $Y(\omega) = kM(\omega)$ , where k is proportionality constant. Hence, for perfect demodulation, the required condition is:

$$[H_{\nu}(\omega - \omega_c) + H_{\nu}(\omega + \omega_c)] = constant for |\omega| \le \omega_m$$

This is called vestigial symmetry condition.



Transmission bandwidth of a VSB-SC signal

#### Fig 1.36 Transmission Bandwidth of VSB-SC

It is seen that the VSB bandwidth exceeds the corresponding SSB bandwidth  $\omega_m$  by  $\omega_v/2$ . Thus, the filter transition bandwidth  $\omega_v$  is an important parameter which decides the VSB bandwidth. It is observed in filter design that spectral components that lie in the transition region suffer distortion causing phase shifts.

### **Magnitude Response of VSB Filter**

Fig. shows the magnitude response of VSB filter.

- > Here observe that fc to fc+W is USB. It's portion from fc to fc +fv is suppressed partially. *fc* to fc W is LSB. It's portion from fc -fv to fc is transmitted as vestige.
- Solution Observe that H(fc)=1/2. And the frequency response  $fc-fv \le H(f) \le fc+fv$  exhibits odd symmetry. The sum of any two frequency components in the range is

 $\label{eq:fc-fv} \begin{array}{c} f_c\text{-}f_v{\leq} \ f{\leq}f_c\text{+}f_v\\ \text{equal to unity. i.e } H(f\text{-}fc) + H(f\text{+}fc) = 1\\ \end{array}$  Phase response is linear



Fig 1.37 Spectrum of VSB

# Advantages:

- 1. Low frequencies, near fc are, transmitted without any attenuation.
- 2. Bandwidth is reduced compared to DSB.

# **Applications:**

VSB is mainly used for TV transmission, since low frequencies near *fc* represent significant picture details. They are unaffected due to VSB.

# **Angle Modulation**

### Definition

We know that amplitude, frequency, or phase of the carrier can be varied by the modulating signal. Amplitude is varied 'in AM. When frequency or phase of the carrier is varied by the modulating signal, then it is called angle modulation, There are two types of angle modulation.

# 1. Frequency Modulation :

When frequency of the carrier varies as per amplitude variations of modulating signal, then it is called Frequency Modulation (FM). Amplitude of the modulated carrier remains constant.

# 2. Phase Modulation :

When phase of the carrier varies as per amplitude variations of modulating signal, then it is called Phase Modulation (PM). Amplitude of the modulated carrier remains constant,

# **Frequency Modulation:**

The frequency of the high frequency carrier signal is carried in accordance with the modulating signal.

$$\begin{split} V_m &= E_m \sin 2\pi f_m t \\ V_c &= E_c \sin 2\pi f_c t \\ V_{fm} &= E_c \sin \left(2\pi f_c t + m_f \sin 2\pi f_m t\right) \\ v_{fm} &= Ec \sin \left(w_c t + m_f \sin w_m t\right) \\ mf \text{ is modulating index of } f_m \end{split}$$

# **Relationship/Difference between FM and PM:**

- The basic difference between FM and PM lies in which property of the carrier is directly varied by modulating signal. Note that when frequency of the carrier varies, phase of the carrier also varies and vice-versa.
- But if frequency is varied directly, then it is called FM.,
- And if phase is varied. directly, then it is called PM.
- The instantaneous phase deviation is denoted by  $\theta$  (t). It is the instantaneous change in phase of the carrier with respect to reference phase. The instantaneous phase of the carrier is precise phase of the carrier at a given instant. It is mathematically expressed as,

Instantaneous phase =  $w_c t + \theta(t)$ 

Here  $\theta(t)$  is the instantaneous phase deviation and Wc is the carrier frequency. Now the instantaneous frequency deviation is defined as

$$=\frac{d(\theta(t))}{dt}=\dot{\theta}(t)$$
 Hz

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**Definition for instantaneous frequency deviation:** It is the instantaneous change in carrier frequency. It is equal to the rate at which instantaneous phase deviation takes place.

Definition of instantaneous frequency: It is the frequency of the carrier t a given instant of time. It is given as

Instantaneous frequency = 
$$\omega_i(t) = \frac{d}{dt} [\omega_c t + \theta(t)]$$
  
=  $\omega_c + \theta'(t)$  rad/sec

Instantaneous phase deivation  $\theta(t)$  is proportional to modulating signal voltage

$$\theta(t) = k e_m(t) \text{ rad}$$

Where K is the deviation sensitivity of phase

#### Similarly the instatueous frequency deviation is proportional to modulating Signal

$$\theta'(t) = k_1 e_m(t) \operatorname{rad/sec}$$

Where k1 is the deviation sensitivity of frequency.

From equation (2), We have

$$\theta(t) = \int \theta'(t) dt = \int k_1 e_m(t) dt$$

Let the modulating signal be given as

 $e_m(t) = E_m \cos \omega_m t$ 

Using the equation in equation (6)

$$\theta(t) = k_1 \int E_m \cos \omega_m t \, dt$$
$$= k_1 \frac{E_m}{\omega_m} \sin \omega_m t$$

The angle modulated wave is mathematically expressed as

$$e(t) = E_c \sin \left[ \omega_c t + \theta(t) \right]$$

Using the value of  $\theta(t)$  in the above equation from equation (7)

**FM equation :** 
$$e(t) = E_c \sin \left[ \omega_c t + \frac{k_1 E_m}{\omega_m} \sin \omega_m t \right]$$

Similarly using the value of  $\theta(t)$  from equation (5) in equation (8) we get

**PM equation :** 
$$e(t) = E_c \sin \left[ \omega_c t + k E_m \cos \omega_m t \right]$$

# FM and PM waveforms:



Fig 1.38 Frequency Modulation

- For FM signal maximum frequency" deviation takes Place when Modulating signal is at positive .and negative peaks.
- For PM signal the maximum frequency. deviation takes place near zero crossings of the modulating signal.
- Both FM anid PM waveforms are identical except the phase shift.

# Definition of Modulation index of PM and FM

The modulation index of PM is given as

M=KE<sub>m</sub>

For FM It is the ratio of maximum frequency deviation ( $\delta$ ) to the modulating frequency ( $f_m$ ).

 $m_f = \frac{Maximum frequency deviation}{Modulating frequency} = \frac{\delta}{f_m}$ 

• The maximum frequency deviation is the shift from centre frequency f<sub>c</sub> when the amplitude of message is maximum.

 $\Delta f = K_1 E_m (Hz)$ 

 $K_1 =$  Deviation sensitivity.

### The Bandwidth of FM:

- By Carson's rule the Bandwidth needed by fm is given as,
  - $B\omega = 2 (\delta + f_m max)$
  - $\delta \rightarrow$  Maximum frequency Deviation

 $f_mmax$  is Maximum modulating frequency.

### **Deviation Ratio :**

The modulation index corresponding to maximum modulating frequency is called deviation ratio.

Maximum frequency deviation

Deviation Ratio =

Maximum modulating frequency

# Frequency Spectrum of angle modualted wave :

• FM and PM analysis is quite complicated. It is derived with the help of Bessel function.  $E_{fm} = E_c \sin (w_c t + mf \cos w_m t)$ 

Using Bessel function this can be expanded as,

 $E_{fm} = A \left\{ J_omf \sin w_c t + J_1mf \left[ \sin (w_c + w_m)t - \sin (w_c - w_m)t \right] \right\}$ 

+  $J_2mf[sin (w_c + 2w_m)t - sin (w_c - 2w_m)t] + J_3mf[sin (w_c + 3w_m)t]$ 

 $-\sin(w_c - 3w_m)t] + J_4mf[\sin(w_c + 4w_m)t - \sin(w_c - 4w_m)t] \dots$ 

 $J_0$ ,  $J_1$ ,  $J_2$ ,  $J_3$  .... Are Bessel functions. The value of this depends on modulation index  $m_f$ .



Fig1.39 Bessel Function Values

From the figure the Bandwidth of FM is given by

$$B = f_c + nf_m - f_c + nf_m BW = 2nf_m$$

### **Bessel Function Table :**

m	JO	J1	J2	J3	J4	J5	J6	J7	J8	J9	J10
0	1	-	-	-	-	-	-	-	-	-	-
0.25	0.98	0.12	-	-	-	-	-	-	-	-	-
0.5	0.94	0.24	0.03	-	-	-	-	-	-	-	-
1	0.77	0.44	0.11	0.02	-	-	-	-	-	-	-
1.5	0.51	0.56	0.23	0.06	0.01	-	-	-	-	-	-
2	0.22	0.58	0.35	0.13	0.03	-	-	-	-	-	-
2.5	-0.05	0.50	0.45	0.22	0.07	0.02	-	-	-	-	-
3	-0.26	0.34	0.49	0.31	0.13	0.04	0.01	-	-	-	-
4	-0.04	-0.07	0.36	0.43	0.28	0.13	0.05	0.02	-	-	-
5	0.18	-0.33	0.05	0.31	0.39	0.25	0.13	0.05	0.02	-	-

## **Classification of FM:**

- 1. Narrowband FM
- 2. Wide band FM

### Narrow band FM:

When the modulation index is less than I, it is called narrowband FM. The FM Equation given by eq. 9 can also be expressed as,

$$e(t) = E_c \cos \left[ \omega_c t + \frac{k_1 E_m}{\omega_m} \sin \omega_m t \right]$$

$$\frac{k_1 E_m}{\omega_m} = m,$$

$$e(t) = E_c \cos \left[2\pi f_c t + m \sin 2\pi f_m t\right]$$

# Expanding the equation

 $e(t) = E_c \cos (2\pi f_c t) \cos [m \sin (2\pi f_m t)] - E_c \sin (2\pi f_c t) \sin [m \sin (2\pi f_m t)]$ 

For narrowband FM, the modulation index, m is very small therefore following approximations can be considered.

 $cos [m sin (2\pi f_m t)] \approx 1$  $sin [m sin (2\pi f_m t)] \approx m sin (2\pi f_m t)$ 

Using this in equation (2)

$$e(t) = E_c \cos \left(2\pi f_c t\right) - m E_c \sin \left(2\pi f_c t\right) \sin \left(2\pi f_m t\right)$$

Expanding

$$e(t) = E_c \cos (2\pi f_c t) + \frac{1}{2} m E_c \left\{ \cos 2\pi (f_c + f_m) t - \cos 2\pi (f_c - f_m) t \right\}$$

This equation gives the spectrum of narrowband FM. Observe that there is carrier frequency fc, upper sideband (fc + fm) and lower sideband (fc - fm).

#### Wide band FM

If the modulation index is higher than 10 it is called as wide band FM

$$e(t) = E_c \cos[2\pi f_c t + m \sin 2\pi f_m t]$$
  
= Re[ $E_c e^{j(2\pi f_c t + m \sin 2\pi f_m t)}$ ]  
= Re[ $E_c e^{j2\pi f_c t} \cdot e^{jm \sin 2\pi f_m t}$ ]

Let  $x(t) = E_c e^{jm\sin 2\pi f_m t}$ , then the above equation becomes

$$e(t) = \operatorname{Re}\left[x(t) e^{j 2\pi f_{c} t}\right]$$

Here  $x(t) = E_c e^{j m \sin 2\pi f_m t}$  is periodic with fundamental frequency of  $f_m$ . It can be expressed with the help of Fourier series as,

$$x(t) = \sum_{n=-\infty}^{\infty} C_n e^{j 2\pi n f_m t}$$

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where

*.*`.

$$C_n = f_m \int_{-\frac{1}{2}f_m}^{\frac{1}{2}f_m} x(t) \ e^{-j \ 2\pi n f_m t} dt$$
  
=  $f_m \int_{-\frac{1}{2}f_m}^{\frac{1}{2}f_m} E_c \ e^{jm \sin 2\pi f_m t} \ e^{-j \ 2\pi n f_m t} dt$   
=  $f_m E_c \int_{-\frac{1}{2}f_m}^{\frac{1}{2}f_m} e^{j(m \sin 2\pi f_m t - 2\pi n f_m t)} dt$ 

put  $y = 2\pi f_m t$  hence the limits will change from  $-\pi to \pi$ .

$$C_n = \frac{E_c}{2\pi} \int_{-\pi}^{\pi} e^{j(m\sin y - ny)} dy$$

The above integral is known as the nth order Bessel function of the first kind. It is given as

$$J_n(m) = \frac{1}{2\pi} \int_{-\pi}^{\pi} e^{j(m \sin y - ny)} dy$$
$$C_n = J_n(m) E_c$$

Using the value of Cn in equation (2)

$$x(t) = \sum_{n=-\infty}^{\infty} J_n(m) E_c e^{j2\pi n f_m t}$$

Using the value x(t) in equation (1)

$$e(t) = \operatorname{Re}\left[\sum_{n=-\infty}^{\infty} J_n(m) E_c \ e^{j 2\pi n f_m t} . e^{j 2\pi f_c t}\right]$$
$$= E_c \sum_{n=-\infty}^{\infty} \operatorname{Re}\left[J_n(m) e^{j 2\pi (f_c + n f_m)t}\right]$$
$$= E_c \sum_{n=-\infty}^{\infty} J_n(m) \cos\left[2\pi (f_c + n f_m)t\right]$$

The Fourier transform of the above equation becomes

$$E(f) = \frac{E_c}{2} \sum_{n=-\infty}^{\infty} J_n(m) \{\delta(f - f_c - nf_m) + \delta(f + f_c + nf_m)\}$$

This equation shows that there are infinite number of components located

fc $\pm$ fm, fc $\pm$ 2fm, fc $\pm$ 3fm.....

# Comparison between narrowband and wideband FM

Sr.no	Narrow band FM	Wide band FM
1	Modulation index is < 1	Modulation index > 10
2	$s(t) = A_c \cos(2\pi f_c t) - mA_c$ $sin(2\pi f_c t) sin(2\pi f_m t)$	$s(t) = A_c \sum_{n=-\infty}^{\infty} J_n(m) \cos \left[ 2\pi (f_c + nf_m) t \right]$
3	Spectrum contains 2 sidebands and carrier	Spectrum cont6ains infinite number of sidebands and carrier
4	BW=2fm	$BW = 2(\delta + f_m(\max))$
5	It is used for mobile communication	It is used for broadcasting and entertainment
6	Maximum deviation =75Hz	Maximum deviation = 5 Hz
7	Range of modulating frequency 30Hz to 15 Kz	Range of modulating frequency30Hz to 3 Kz

Comparison between FM and PM

	Frequency modulation	Phase modulation
1	The maximum frequency deviation depends	The maximum phase deviation depends only
	upon amplitude of modulating voltage and	upon the amplitude of modulating voltage
	modulating frequency	
2	Frequency of the carrier is modulated by	Phase of the carrier is modulated by modulating
	modulating signal	signal
3	Modulation index is increased as modulation	Modulation index remains same if modulating
	frequency is reduced and vice versa	frequency is changed
4	Noise immunity is bette than AM and PM	Noise immunity is better than AM but worse
		than FM

5	FM is widely used	PM is used in some mobile systems.

### **Generation of FM waves:**

Fm Modulators: There are 2 types of FM modulators.

- 1. Direct Method
- 2. Indirect Method



Direct FM Modulators : In this type the frequency of the carrier is varied directly by the modulating signal.

Indirect FM Modulators: In this type FM is obtained by phase modulation of the carrier.



a) FM from PM b) PM from FM

**Generation of Narrow band FM:** 



Fig 1.41 Generation of Narrowband FM

### **Direct FM reactance modulator:**



### Fig 1.42 Direct FM reactance Modulator

- It behaves as reactance across terminal A-B.
- The terminal A-B of the circuit may be connected across the tuned circuit of the oscillator to get fm o/p.
- The varying voltage (modulating voltage) V, across the terminals A-B changes the reactance of FET.
- This charge in reactance can be inductive or capacitive.
- Neglecting the gate current, let the current through C & R be  $I_1$ .
- At the carrier freq. the reactance of C is much larger than

$$R \& I_{1} = \frac{V}{R + 1/jwc}$$

$$Jwc \gg R$$

$$I_{1} = jwcV$$
From the Circuit,
$$V_{g} = I_{1}R = jwcrv$$

$$I_{d} = g_{m}v_{g}s = g_{m}V_{g}$$

$$I_{d} = jwcRg_{m}V$$
From the circuit impedance of the FET is,
$$Z = \frac{V}{Id}$$

$$= \frac{V}{Id}$$

$$I_{d} = \frac{V}{jwCR gm V} = \frac{1}{jw (gmCR)} = \frac{1}{jw (C_{eq})}$$

- The impedance of FET is capacitive.
- By carrying the modulating voltage across FET, the operating paint  $g_m$  can be varied and hence  $C_{eq}$ .
- This change in the capacitance will change the frequency of the oscillator.

### **Frequency Modulation using Varactor diode.**



Fig 1.43 Varactor Diode for FM Generation

- We know that the junction capacitance of the varactor diode changes as the reverse bias across it is varied.
- L<sub>1</sub> & C<sub>1</sub> forms the tank circuit of the carrier oscillator.
- The capacitance of the varactor diode depends on the fixed bias set by  $R_1 \& R_2 \& AF$  modulating signal.
- Either R1 or R2 is made variable.
- The radio frequency choke [RFC] has high reactance at the carrier frequency to prevent carrier signal from getting into the modulating signal.
- At +ve going modulating signal adds to the reverse bias applied to the varactor diode D, which decreases its capacitance & increases the carrier frequency.
- A -ve going modulating signal subtracts from the bias, increasing the capacitance, which decreases the carrier frequency.

### **Direct FM Transmitters :**



Fig 1.44 Direct FM Transmitter

- Fig. shows the FM Crosby transmitter with an AFC loop. (Automatic frequency correction loop).
- The Frequency modulator can be either a reactance modulator or voltage controlled oscillator.
- The carrier freq is 5.1MHz. which multiplies by 18 in three steps to produce a final frequency of 91.8 MHz.
- When the frequency modulated carrier is multiplied, its frequency & phase deviations are also multiplied.
- The rate at which the carrier is deviated is unaffected by the multiplication process. Hence the modulation index is multiplied.
- When an angle modulated carrier is heterodyned with another freq in a non linear mixer, the carrier can either be up converted or down converted.

# **AFC loop :**



Fig. 2.3.1 Typical AFC circuit

# Fig 1.15 Typical AFC Circuit

- The purpose of the AFC loop is the achieve near crystal stability of the transmit carrier freq. without using a crystal in the carrier oscillator.
- The cassier frequency is mixed with a local oscillator freq and then down converted in freq. & the fed to a frequency discriminator.
- Frequency discriminator is a device whose o/p voltage is proportional to difference b/w i/p freq and its resonant freq.
- Discriminator responds to low freq changes in the carrier center freq because of master oscillator freq drift.
- When the discriminator responds to frequency deviation, the feedback loop would cancel the deviation and this remove the modulation.
- The dc correction voltage is added to the modulating signal to automatically adjust the master oscillator's centre frequency to compensate for low freq drift.

### **PLL Direct FM transmitter:**



### Fig 1.46 PLL - Direct FM Transmitter

- Fig shows a wide band FM transmitter.
- The VCO o/p freq is divided by N & fed bark to the PLL phase comparator, where it is compared to a stable reference freq.
- The phase comparator generator a correction voltage that is proportional to the difference b/w the 2 frequencies.
- The correction voltage is added to the modulating signal & applied to the VCO i/p.
- The correction voltage adjusts the VCO centre freq to its proper value.
- The LPF prevents the changes in the VCO o/p frequency due to the modulating signal from being converted to a voltage & fed back to VCO.
- The LPF also prevents the loop from locking onto a side frequency.

### **Indirect Fm transmitter**



Fig 1.47 Indirect FM transmitter



# Fig 1.48 Phasor Diagram of indirect method of FM Generation

- Here the modulating signal directly deviates the phase of the carrier, which indirectly changes the frequency.
- The carrier source is a crystal oscillator hence stability can be achieved without a AFC.
- A carrier is phase shifted to 90<sup>0</sup> & fed to the Balanced modulator. Where it is mixed with the i/p modulating signal.
- The o/p of balanced modulator is DSBSC.
- The o/p of Balanced modulator is combined with original carrier in the combining N/W. to produce a low index, phase modulated wavefrom.
- Fig (b) shows phasor of original carrier, modulating signal and the resultant Vector.
- Fig (b) shows the phasors for the side freq. components of the suppressed carrier wave. As suppressed carrier is out of phase with Vc, the upper & Lower side bands combine to produce Vm 90° with Vc.
- The phase modulated signal is obtained by vector addition of carrier and modulating signal.
- Modulating signal vector adds to the carrier OA with  $90^0$  phase Shift.
- The resultant phase modulated vector is OB with phase shift  $\theta$ .
- This works only if both have the same frequency. The means carrier & modulating signal should have same frequency. Under this condition phase modulation produces FM o/p.

# **FM Demodulators / Detectors**

# FM demodulator must satisfy the following requirements

- It must convert the frequency variations into amplitude variations
- This conversion must be linear and efficient.
- The demodulator circuits must be insensitive to amplitude changes.
- It should not be too critical in its adjustment and operation.

# **Types of FM demodulator:**

- Round Travis Detector or Balanced discriminator.
- Foster Seley Discriminator or Phase discriminator.
- Ratio Detector.

# Slope Detector / Round Travis Detector :



# Fig 1.49 Balance Slope detector and its characteristics

- Consists of 2 identical circuit connected back to back.
- FM signal is applied to the tuned LC circuit.
- Two tuned LC circuits are connected in series.
- The inductance of the secondary tuned LC circuit is coupled with the inductance of the primary LC circuit this forms a tuned transformer.
- Upper tuned circuit is  $T_1$  & lower tuned circuit is  $T_2$ .
- I/P side LC is tuned to be

 $T_1 \text{ is tuned to } f_c + \delta f \ \text{ - max freq fm.}$ 

 $T_2$  is tuned to  $f_c$  -  $\delta f\,$  - max freq fm.

- Secondary of  $T_1 \& T_2$  are connected to diodes  $D_1 \& D_2$  with RC loads.
- The total o/p is equal to difference b/w Vo1 & Vo2.
- When i/p freq is fc, both T1 & T2 produce the same voltage hence o/p = 0
- When i/p freq is f<sub>c</sub> + δf, the upper circuit T<sub>1</sub> produces maximum voltage since it is tuned to this freq. Hence this produces maximum votalge.

 $V_{01}$  is high compared to  $V_{02}$ .

Vout =  $V_{01}$  -  $V_{02}$  is positive for fc +  $\delta f$ .

• When i/p freq is  $f_c - \delta f$ . T<sub>2</sub> produces maximum signal since it is tuned to it. But T<sub>1</sub> produces minimum voltage. Hence o/p Volt = V<sub>01</sub> - V<sub>02</sub> is negative. Thus we get a modulating signal.

## Foster - Seeley Discriminator :



Fig 1.50 Basic Foster- Seeley Discriminator & Voltage generator equivalent circuit

- The primary voltage is coupled through  $C_3 \& RFC$  to the centre tap on the secondary.
- The capacitor C3 passes all the frequencies of Fm. The voltage  $V_1$  is generated across RFC.
- RFC offers high impedance to frequencies of Fm.



- Fig 1.51 (a) At center frequency, phase shift between  $V_1$  and  $V_2$  is 90°. Hence  $|V_{D1}| = |V_{D2}|$ 
  - (b) For the frequencies above center frequency, the phase shift between  $V_1$  and  $V_2$  is reduced. Hence  $|V_{D1}| > |V_{D2}|$
  - (c) For frequencies below center frequency, the phase shift between  $V_1$  and  $V_2$  is increased. This makes  $|V_{D1}| < |V_{D2}|$
- The voltage V<sub>1</sub> thus appears across centre tap of secondary and ground also.
- The voltage of secondary is  $V_2$  & equally divided across upper half & lower half of the secondary.
- In the figure the voltage across diode  $D_1$  is  $V_{DI} = V_1 + 0.5 V_2$  and that across  $D_2$  is  $V_{D2} = V_1 + 0.5 V_2$
- The o/p of upper rectifier is  $V_{01}$  and lower rectifier is  $V_{02}$ .
- The net  $o/p V_0 = V_{01} V_{02} \cong V_0 = |V_{D1}| |V_{D2}|$
- At carrier frequency  $V_{D1} \ge V_{D2}$  are equal hence the net o/p of the discriminator will be zero.
- When the i/p frequency increases above fc the phase shift b/w  $V_1 \& V_2$  reduces  $|V_{D1}| > |V_{D2}|$  hence  $V_{01} = |V_{D1}| - |V_{D2}|$  will be +ve.
- When the i/p frequency reduces below fc then  $|V_{D1}| > |V_{D2}|$  hence  $|V_{D1}| |V_{D2}|$  will be -ve.

2021-2022

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#### **Ratio detector :**





Ratio detector can be obtained by sight modifications in the foster-Seeley discriminator. Fig shows the circuit diagram of ratio detector. As shown in the diagram the diode  $D_2$  is reversed, and output is taken from different points. In the above circuit the regular conversion from frequency to phase shift and phase shift to amplitude takes place as in faster–Seeley discriminator. The polarity of voltage in the lower capacitor is reversed. Hence the voltages  $V_{01}$  and  $V_{02}$  across two capacitors add. (Note that these voltages subtract in faster-seely circuit). And we know that when  $V_{01}$  increases,  $V_{02}$  decreases and vice-versa as we have seen in faster-Seeley circuit. Since,  $V_0'$  is sum of  $V_{01}$  and  $V_{02}$ , it remains constant. From the circuit of Fig we can write two equations for the output voltage  $V_0$  (Note that  $V_0$  is the net output voltage and taken across points A and B). The First equation will be,

$$V_0 = \frac{1}{2} V_0 - V_{02}$$

and  $V_0 = -\frac{1}{2} V_0' - V_{01}$ 

adding the above two equations,

$$2 V_0 = V_{01} - V_{02}$$
$$V_0 = \frac{1}{2} (V_{01} - V_{02})$$

Since  $V_{01} \approx |V_{D1}|$  and  $|V_{02}|$  above equation will be,

$$V_0 = \frac{1}{2} (|V_{D1}| - |V_{D2}|)$$

- Here  $V_{D1}$  &  $V_{D2}$  are obtained as discussed earlier in foster seeley circuit.
- From the equation we know that the output of ratio detector is half compared to that of Foster-Seeley circuit

- As frequency increases above fc'  $|V_{D1}| > |V_{D2}|$  hence o/p is +ve.
- III <sup>rly</sup> as frequency decreases below  $fc = |V_{D2}| > |V_{D1}|$ , hence o/p is -ve.

## Advantage :

• Reduced fluctuations in the o/p voltage compared to foster seeley circuit

PLL Demodulator circuit



Fig 1.53 PLL- Demodulator circuit

- Fig. shows the block diagram of PLL FM demodulator.
- The output frequency of VCO is equal to the frequency of unmodulated carrier.
- The phase detector generates the voltage which is proportional to difference between the FM signal and VCO output.
- This voltage is filtered and amplified. It is the required modulating voltage.
- Here frequency correction is not required in VCO since it is already done at transmitter

**Comparison of FM and AM** 

	Amplitude Modulation	Frequency Modulation
1.	Amplitude of the carrier is varied	Frequency of the carrier is varied
	according to amplitude of modulating	according to amplitude of the
	signal.	modulating signal.
2	An has noon fidality due to normany	Since the handwidth is large
Ζ.	Am has poor indenty due to narrow	Since the bandwidth is large,
	bandwidth.	fidelity is better.
3.	Most of the power is in carrier hence less	All the transmitted power is useful.
	efficient.	
4.	Noise interference is more.	Noise interference is minimum.
5.	Adjacent Chennai Interference is present	Adjacent Chennai Interference is
		avoided due to guard bands.

6.	Am Broadcast operates in MF and HF range	FM Broadcost operates in VHF and UHF range.
7.	In Am only carrier and two sidebands are present	Infinite number of sidebands are present
8.	The transmission equipment is simple.	The transmission equipment is complex.
9.	Transmitted power varies according to modulation index.	Transmitted power remains constant irrespective of modulation index.
10.	Depth of modulation have limitation. It can not be increased above I.	Depth of modulation have no limitation. It can be increased by increasing frequency deviation.